

Mining and Processing Biomedical Data

Dr. rer. nat. Krisztian Buza

adiunkt naukowy

Faculty of Mathematics, Informatics and Mechanics

University of Warsaw, Poland

chrisbuza@yahoo.com

Matrix completion techniques

Matrix completion for biomedical tasks

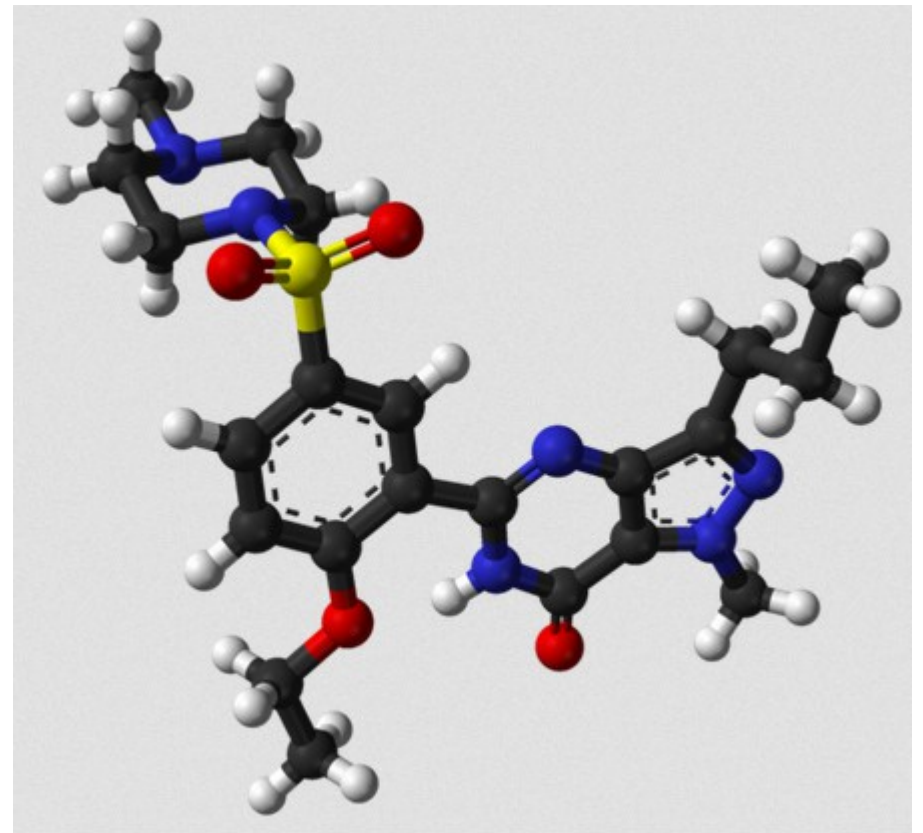
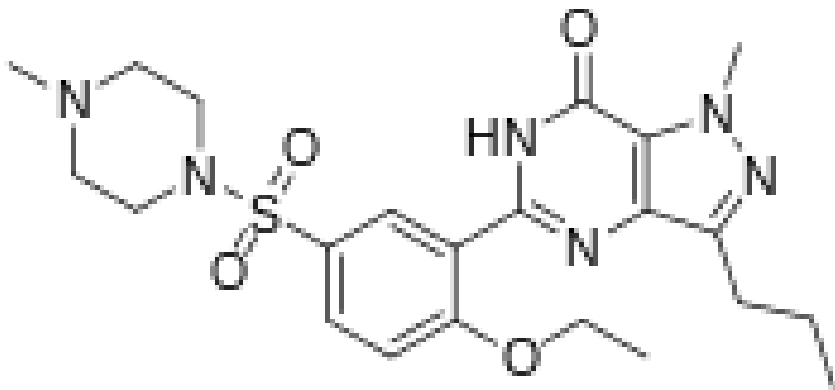
- Drug-target prediction
- Prediction of side effects of drugs
- Link prediction in biological networks
- Analysis of DNA-methylation in case of cancerous tissues

Module overview

- Lecture 3A – Motivation, „side effect“ of Viagra
- Lecture 3B – Matrix multiplication
- Lecture 3C – Matrix factorisation (MF) based on the minimization of sum of squared errors with gradient descent
- Lecture 3D – Link prediction
- Lecture 3E – Restricted Boltzmann Machines (RBMs)
- Lecture 3F – Drug-target prediction with RBMs, MF for the analysis of DNA-methylation

Example: „side effects“ of Viagra (Sildenafil)

See also <http://en.wikipedia.org/wiki/Sildenafil>



Images from Wikipedia are used on this slide. Licence info:

<http://en.wikipedia.org/wiki/File:Sildenafil.svg>

<http://en.wikipedia.org/wiki/File:Sildenafil-from-xtal-3D-balls.png>

Lessons learned from the example

- Some side effects of a drug may potentially not be discovered during clinical trials
 - e.g. because these side effects are only present under certain conditions
- The side effect of a drug may be even more relevant than the effect the drug was designed to have
- Computational methods may predict potential side effects

Prediction of drug-target interactions

- Assume that we are given a drug. This drug is unlikely to interact with a randomly selected target, e.g., probability of the interaction is 0.1%.
- Due to the **large amount** of possible targets, the expected value of the number of interactions may be in the order of dozens!
- Computational methods for drug-target interaction may generate useful hypothesisises about which drug-target interactions should be tested.

Multiplication of matrices

Example: Multiplication of 2x2 matrices

$$\begin{pmatrix} 3 & 8 \\ 2 & 0 \end{pmatrix} \begin{pmatrix} 0 & 2 \\ 5 & 7 \end{pmatrix}$$

Example: Multiplication of 2x2 matrices

$$\begin{bmatrix} 3 & 8 \\ 2 & 0 \end{bmatrix} \times \begin{bmatrix} 0 & 2 \\ 5 & 7 \end{bmatrix} = \begin{bmatrix} & \\ & \end{bmatrix}$$

Example: Multiplication of 2x2 matrices

„row times column“

$$\begin{pmatrix} 3 & 8 \\ 2 & 0 \end{pmatrix} \times \begin{pmatrix} 0 & 2 \\ 5 & 7 \end{pmatrix} = \begin{pmatrix} \boxed{} \\ \end{pmatrix}$$

$$(3 \times 0) + (8 \times 5) = 0 + 40 = 40$$

Example: Multiplication of 2x2 matrices

„row times column“ $(3 \times 2) + (8 \times 7) = 6 + 56 = 62$

$$\begin{bmatrix} 3 & 8 \\ 2 & 0 \end{bmatrix} \times \begin{bmatrix} 0 & 2 \\ 5 & 7 \end{bmatrix} = \begin{bmatrix} 40 & \\ & \end{bmatrix}$$

Example: Multiplication of 2x2 matrices

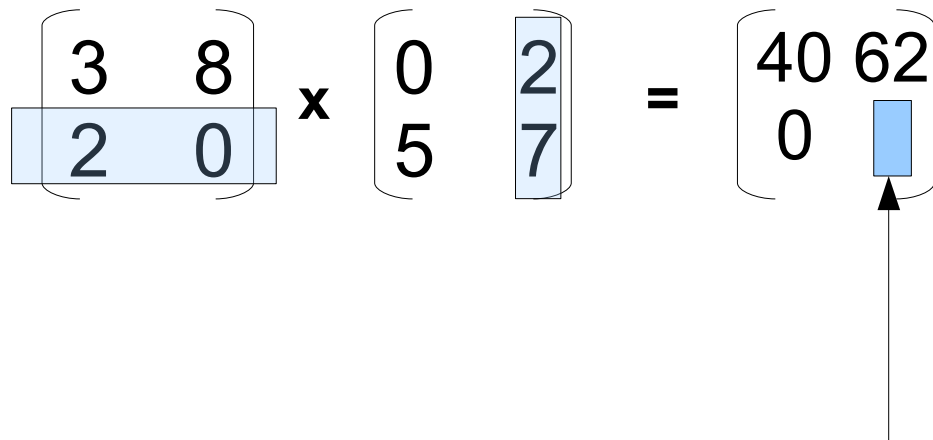
„row times column“

$$\begin{pmatrix} 3 & 8 \\ 2 & 0 \end{pmatrix} \times \begin{pmatrix} 0 & 2 \\ 5 & 7 \end{pmatrix} = \begin{pmatrix} 40 & 62 \\ \color{blue}{} & \end{pmatrix}$$

$(2 \times 0) + (0 \times 5) = 0 + 0 = 0$

Example: Multiplication of 2x2 matrices

„row times column“

$$\begin{pmatrix} 3 & 8 \\ 2 & 0 \end{pmatrix} \times \begin{pmatrix} 0 & 2 \\ 5 & 7 \end{pmatrix} = \begin{pmatrix} 40 & 62 \\ 0 & \color{blue}{\boxed{}} \end{pmatrix}$$


$$(2 \times 2) + (0 \times 7) = 4 + 0 = 4$$

Example: Multiplication of 3x3 matrices

„row times column“

$$\begin{pmatrix} 8 & 6 & 12 \\ 3 & 9 & 1 \\ 0 & 7 & 21 \end{pmatrix} \times \begin{pmatrix} 1 & 9 & 2 \\ 5 & 10 & 1 \\ 6 & 3 & 7 \end{pmatrix} = \begin{pmatrix} & & \\ & & \\ & & \end{pmatrix}$$

$$(3 \times 1) + (9 \times 5) + (1 \times 6) = 3 + 45 + 6 = 54$$

Example: Multiplication of 3x3 matrices

„row times column“

$$\begin{array}{l} \text{\textit{i}-th row} \rightarrow \end{array} \begin{pmatrix} 8 & 6 & 12 \\ 3 & 9 & 1 \\ 0 & 7 & 21 \end{pmatrix} \times \begin{array}{l} \text{\textit{j}-th column} \\ \downarrow \end{array} \begin{pmatrix} 1 & 9 & 2 \\ 5 & 10 & 1 \\ 6 & 3 & 7 \end{pmatrix} = \begin{pmatrix} & & \\ & & \\ & & \end{pmatrix}$$

Element in the i -th row and j -th column:
product of the i -th row of the first matrix
and the j -th column of the second matrix